

On “Counterfactual Attitudes and Multi-Centered Worlds” ([Ninan 2012](#))

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“... I think the generality of my title [“Attitudes *De Dicto* and *De Se*”] is well justified. I’m not sure anything is left out – perhaps some ill-understood attitudes of **imagining**, conceiving, contemplating, or entertaining a thought.” ([Lewis 1979](#): 529, my emphasis)

1 The Lewisian View and Ninan’s Challenge

- Intuitive basis of *centered worlds*:
 - A god, looking down on the world, can say everything there is to say about that world by specifying the states of affairs, laws, modal properties, etc.
 - This model is inappropriate to capture the rational behavior of agents located *in* a world
 - With an agent located within that world, once they know what the world is like needs to know which of the individuals in that world they are
- Lewisian’ *De Se* Semantics:

x believes, at w, t , that she (herself) is a spy:

 - $\{\langle w', t', x' \rangle \mid x' \text{ has at } w', t' \text{ all properties } x \text{ self-ascribes in } w, t\}$
 $\subseteq \{\langle w', t', x' \rangle \mid x' \text{ is a spy at } w', t'\}$
- Why isn’t x the center of her beliefs?
 - *Essential properties problem*: x may not believe she came from a sperm and egg ([Lewis 1983](#): 15)
 - ▶ But, any world where x exists, x came from a sperm and egg
 - ▶ So the set of centered worlds where x has all self-ascribed properties is identical to set of centered worlds where x has all self-ascribed properties and essential/necessary ones too

- **Question 1**: consider an agent x which self-ascribes being identical to Bush, and also fails to believe he came from a sperm and egg.
 - In order for x' to have the first property in w' , they have to be Bush, but the second property is incompatible with this.
- **Lewisian *De Re* Semantics**:

Ralph believes, at w, t , of Ortcutt, that he is a spy:

 - There is an acquaintance relation R :
 - (a) Ralph bears R uniquely to Ortcutt at w, t
 - (b) $\{\langle w', t', x' \rangle \mid x' \text{ has at } w', t' \text{ all properties Ralph self-ascribes in } w, t\}$
 $\subseteq \{\langle w', t', x' \rangle \mid \text{the } y \text{ to which } x' \text{ bears } R \text{ in } w', t' \text{ is a spy at } w', t'\}$
 - R is: seeing-sneak-around-on-the-dock
- Relation between *de re* and *de se*:
 - “That suggests that a *de se* belief is also a *de re* belief about oneself. This suggestion is vindicated by Lewis’s theory if we count the relation of identity as a relation of acquaintance, and take a *de se* belief to be a *de re* belief about oneself relative to the relation of identity.” ([Ninan 2012](#): 13, on Lewis’ theory)
- **Question 2**: how does this deal with standard cases of *de re* beliefs about oneself that fail to be *de se* beliefs?
 - Kaplan sees someone in the window with his pants on fire, not realizing it is his reflection
 - Perry, following a sugar trail he is unknowingly creating in the grocery store, thinks that this guy is making a mess
 - Further, if an acquaintance relation is just any relation by which information is being reliably transmitted (at that world-time), doesn’t the identity relation always count?

Ninan’s challenge:

- What’s the content of the following attitude attribution: Ralph imagined that he did not see Ortcutt sneaking around on the dock?
- R is not instantiated in this counterfactual scenario, so clause (b) in the Lewisian semantics fails
 - But R is the only relation satisfying (a)!
- *The gist*: which acquaintance relations hold are contingent and so vary in counterfactual scenarios, but Lewis’ theory makes those relations a necessary condition for the truth of *de re* attributions

2 Multi-Centered Worlds Solution

- [Ninan \(2012\)](#) proposes to distinguish possibilities more finely than centered worlds: multi-centered worlds

Old	$\langle w', t', x' \rangle$
New	$\langle w', t', \underbrace{\{ \langle \text{Ralph}, Q \rangle, x' \rangle, \langle \text{Ortcutt}, R \rangle, y' \rangle, \dots \}}_f \rangle$

- Centers are replaced with *tagging functions* f
- Intuitively, f :
 - ▶ *Takes*: things x is acquainted with in w and a way x is acquainted with it (an *acquaintance pair*)
 - ▶ *Returns*: that thing's 'representative' in w'
- In practice, the domain the various f 's is generally taken to be the acquaintances/relations of the agent whose attitudes we are modeling - so they stay constant across multi-centered worlds
 - ▶ In practice, the domain of all tagging functions is the *acquaintance set* of the agent being modeled
 - ▶ What varies: individual an acquaintance pair is mapped to

- **Multi-Centered De Re Semantics** (informal version):

x imagines, at w, t , of Orcutt that he (relative to R) is not dock-sneaking:

- $Im_{x,w,t} \subseteq \{ \langle w', t', f' \rangle \mid f'(\text{Ortcutt}, R) \text{ is not dock-sneaking}_{w',t'} \}$
 - ▶ $Im_{x,w,t}$: x 's imagination worlds in w, t
 - ▶ $Im_{x,w,t} = \{ \langle w', t', f' \rangle \mid \text{dom } f' = \{ \langle a_0, A_0 \rangle, \dots, \langle a_n, A_n \rangle \} \}$
& $f'(\langle a_0, A_0 \rangle), \dots, f'(\langle a_n, A_n \rangle)$ are related $_{w',t'}$ as x imagines $_{w,t}$
- Unlike Lewis' semantics: R needn't hold between x and Orcutt at w, t
 - Though we could add that in to analyze *believes*
- **Question 2** (again): since it seems so easy for the identity acquaintance relation to hold, how does it fail in cases of *de re* beliefs about oneself that aren't *de se*?
 - If identity acquaintance relations aren't so easy, what more is there to them than reliable information transmission?
- This finer conception of content addresses Ninan's challenge
- Let's assume Ninan's challenge is to be addressed by refining content and re-tuning the semantics of attitude verbs
- **My Main Question**: are tagging functions the best tool for doing this?

3 Worries about Multi-Centered Content

- **Worry 1**: tagging functions do not play the theoretical role of *indices*, like w and t , so they don't belong with them in a theory of *content*
 - One role of indices is to capture the ways in which our information can be *partial*
 - ▶ w : we can fail to know which total state the world is in
 - ▶ t : we can know that total state, but not what stage we're at
 - ▶ x : we can know which world-stage we're in, but not which individual we are (Lewis)
 - ▶ f : we can know which world-stage we're in, but not (i) what we're acquainted with and how, or if so, (ii) who's playing the role of that acquaintance in this world...
 - ▷ Variation in the *domain* of the tagging functions is not exploited, so type (i) partiality is not useful
 - ▷ Type (ii) is the same as Lewis' model
 - Another role: an essential component for determining truth
 - ▶ [Ninan \(2012: 42-3\)](#) relativizes truth to **assignment functions**
 - ▷ The tagging functions implicated in an agent's attitudes are used to set the values of the assignment function
 - ▷ Tagging functions not essential for determining truth!
 - Indices are possibilities communicated content distinguishes btwn
 - ▶ But multi-centered contents are often incommunicable, as [Ninan \(2012: 38n5\)](#) admits
 - ▶ When I believe I am hungry I believe: $\{ \langle w, t, f \rangle \mid f(\text{WS}, \text{identity}) \text{ is hungry}_{w,t} \}$
No one else can believe a proposition containing this f
- **Worry 2**: what does it mean to have a world (partially) centered on an individual that doesn't exist there?
- **Worry 3**: a certain subset of the multi-centered worlds intuitively model an agent's perspective on a world, but most don't. Does this suggest that this conception of content is too general?
 - In practice, all individuals used as centers are individuals from the world of evaluation
 - All are acquaintances of an agent named in the attribution
 - Tagging functions capture a particular agent's *perspective*
 - We're in w, t , and are acquainted only with ourselves; a doesn't exist here. Where in logical space, with respect to us, is: $\langle w', t', \{ \langle \langle a, Q \rangle, b \rangle, \dots \} \rangle$

- **Worry 5:** can we make sense of plural attributions like *We (all) believe we are here in NJ*?
 - Desiderata: analysis should entail I believe *de se* that I'm in NJ, that Ernie believes *de se* that he's in NJ, etc.
 - ▶ Can't say this if we know Ernie thinks he is at a concert in NYC but that the conference magnate he heard about is in NJ
 - *Problem:* treating *we* as *I+you*, multi-centered view only predicts *de se* reading for speaker

4 Another Solution without the Worries?

- Don't let these worries rain on a productive research program, unless there's another party?
- Where's is it? Nowhere, completely: [Kamp \(2011\)](#), [Cumming \(2008, to appear\)](#), [Bittner \(2012\)](#), [Kaplan \(1968\)](#)
 - Not actually sure it's happening, but worth looking into
- [Ninan \(2012\)](#) already makes essential use of variable assignments in his formal semantics:
 - Names and pronouns are treated as variables, including *I* (§5.2)
- Basic picture:
 - **Content:** sets of world-assignment pairs ('discourse content') ([Dekker 1993](#); [Groenendijk et al. 1996](#))
 - ▶ Assignments characterize a 'reference relation' between symbols and referents
 - ▷ $\langle w, g \rangle$: w is how the non-linguistic world is, g is how the symbols refer to things in that world ([Cumming 2008](#))
 - Attitudes: an agent can learn about the non-linguistic world (eliminate all possibilities like $\langle w, \dots \rangle$) or the reference relation (eliminate all possibilities like $\langle \dots, g \rangle$)
 - *De Dicto:* reference relations compatible with subject's beliefs are used to interpret rigid designators in scope of *believes*
 - ▶ That is, attitude verbs are *assignment-shifters*
 - *De Re:* projecting the reference relation in use in the context, onto the worlds from agent's 'belief set'
 - *De Se:* assignment function has a special variable l which can only be assigned to speaker of context ([Kamp 2011](#); [Bittner 2012](#))
 - ▶ Some languages contain attitude verbs that shift even this variable (e.g. [Schlenker 2003](#); [Bittner 2012](#))

- The *de re* idea in a little more detail, for x believes of Ortcutt that he is a spy:
 - Basic idea: if x referred as we do with Ortcutt then the proposition expressed by Ortcutt is a spy would be true in all of x 's belief world-assignment pairs
- **De Re Semantics:**

$$\llbracket x \text{ believes of Ortcutt that he is a spy} \rrbracket = \{ \langle w, g \rangle \mid \langle w', g' \rangle \in B_{g(x), w} \ \& \ g' \in g^{\sim w'} \ \& \ \langle w', g' \rangle \in \llbracket \text{Ort is a spy} \rrbracket \ \& \ g(\text{Ort}) \in D_{w'} \}$$
 - $g^{\sim w'}$ is the set of projections of g onto w' :
 - ▶ Every projection agrees with g when $g(v)$ exists in w'
 - ▶ Otherwise, a projection has a suitable ersatz for $g(v)$
 - ▷ Lots of options to explore for doing this
 - ▷ Acquaintance relations, counterparts, contextually salient property maximization, etc.
 - If we didn't care about the essential properties problem, we could just alter x 's g' to match g on Ort
- Getting around essential properties problem:
 - In worlds where Ortcutt doesn't exist, g' can assign Ortcutt to something else and still, technically, be rigid
 - One worry: do Ralph's anti-science belief worlds contain actual Ortcutt, who came from a sperm-and-egg, as well as miraculous-Ortcutt who was assembled in the womb from fairy-wings?
- *De re* imagination requires no special treatment, it's just a case where projection will very likely be necessary
- Getting around the incommunicability of *de se* contents:
 - For this approach to work to Frege's problem, the symbols in the reference relation need to be an agent's *mental symbols*
 - Since no two agent's share mental symbols they don't share discourse content
 - However, one can tell a story about two speakers who share a public language can come into alignment such that we can say they *carry the same information* ([Cumming to appear](#))
 - For names, roughly:
 - ▶ They have aligned signaling strategies: if x encodes mental symbol s_x with a and y construes a with their mental symbol s_y , then y uses a to encode s_y and x construes it with s_x
 - For indexicals, the inverse!
 - So communicating *de se* contents is the same as communicating *de dicto* contents

References

- BITTNER, M (2012). 'Perspectival Discourse Referents for Indexicals.' In H GREEN (ed.), *Proceedings from SULA 7*. URL http://www.rci.rutgers.edu/~mbittner/bitt12_sula7.pdf.
- CUMMING, S (2008). 'Variablism.' *Philosophical Review*, **117**(4): 525-554.
- CUMMING, S (to appear). 'Coordinating in the Dark: from private symbols to Fregean content.' *Philosopher's Imprint*. URL <https://dl.dropbox.com/u/31660624/kpuzzle-8-12.pdf>.
- CUMMING, S (to appearb). 'Creatures of Darkness.' *Analytic Philosophy*. URL <http://dl.dropbox.com/u/31660624/creatures-7-11.pdf>.
- DEKKER, P (1993). *Transsentential Meditations*. Ph.D. thesis, University of Amsterdam, Amsterdam.
- GROENENDIJK, J, STOKHOF, M & VELTMAN, F (1996). 'Coreference and Modality.' In S LAPPIN (ed.), *The Handbook of Contemporary Semantic Theory*, 179-213. Oxford: Blackwell Publishers.
- KAMP, H (2011). 'Representing *De Se* Thoughts and Their Reports.' Ms. University of Stuttgart, URL http://nass11i2012.com/files/kamp_2011.pdf.
- KAPLAN, D (1968). 'Quantifying In.' *Synthese*, **19**(1/2): 178-214.
- LEWIS, DK (1979). 'Attitudes *de Dicto* and *de Se*.' *The Philosophical Review*, **88**: 513-543.
- LEWIS, DK (1983). 'Individuation by Acquaintance and by Stipulation.' *The Philosophical Review*, **92**(1): 3-32. URL <http://www.jstor.org/stable/2184519>.
- NINAN, D (2012). 'Counterfactual attitudes and multi-centered worlds.' *Semantics and Pragmatics*, **5**(5): 1-57.
- SCHLENKER, P (2003). 'A Plea for Monsters.' *Linguistics and Philosophy*, **26**(1): 29-120.