

## Malink's (2006) System $\mathcal{A}$

### Axioms of $\mathcal{A}$ (Malink 2006: 115)

- (ax<sub>1</sub>)  $\Upsilon aa$   
 (ax<sub>2</sub>)  $\Upsilon ab \wedge \Upsilon bc \supset \Upsilon ac$   
 (ax<sub>3</sub>)  $\hat{\mathbf{E}}ab \supset \Upsilon ab$   
 (ax<sub>4</sub>)  $\mathbf{E}ab \wedge \Upsilon bc \supset \mathbf{E}ac$   
 (ax<sub>5</sub>)  $\tilde{\mathbf{E}}ab \wedge \Upsilon bc \supset \tilde{\mathbf{E}}ac$

### Definitions of $\mathcal{A}$ (Malink 2006: 115)

- (df<sub>1</sub>)  $\Sigma a := \exists z \mathbf{E}za$   
 (df<sub>2</sub>)  $\mathbf{K}ab := \Sigma a \wedge \Sigma b \wedge \neg \exists z (\Upsilon az \wedge \Upsilon bz)$   
 (df<sub>3</sub>)  $\Pi ab := \neg(\Sigma a \wedge \Sigma b) \wedge \neg \mathbf{E}ab \wedge \neg \mathbf{E}ba \wedge ((\Sigma a \vee \Sigma b) \supset \exists z (\Upsilon az \wedge \Upsilon bz))$   
 (df<sub>4</sub>)  $\bar{\Pi}ab := \Pi ab \vee \Upsilon ab$   
 (df<sub>5</sub>)  $\hat{\mathbf{E}}ab := \mathbf{E}ab \vee \tilde{\mathbf{E}}ab$   
 (df<sub>6</sub>)  $\hat{\Sigma}a := \exists z \hat{\mathbf{E}}za$   
 (df<sub>7</sub>)  $\bar{\mathbf{E}}ab := \mathbf{E}ab \vee (\Sigma a \wedge \Upsilon ab)$

### Abbreviations for Modal Syllogistic Copulae in $\mathcal{A}$ (Malink 2006: 116)

$\mathbb{X}^a ab := \Upsilon ab$	$\mathbb{M}^a ab := \forall z (\Upsilon bz \supset \bar{\Pi}az)$
$\mathbb{X}^e ab := \forall z (\Upsilon bz \supset \neg \Upsilon az)$	$\mathbb{M}^e ab := \forall z (\Upsilon bz \supset \neg \bar{\mathbf{E}}az) \vee \forall z (\Upsilon az \supset \neg \bar{\mathbf{E}}bz)$
$\mathbb{X}^i ab := \exists z (\Upsilon bz \wedge \Upsilon az)$	$\mathbb{M}^i ab := \exists z (\Upsilon bz \wedge \bar{\Pi}az)$
$\mathbb{X}^o ab := \neg \Upsilon ab$	$\mathbb{M}^o ab := \neg \bar{\mathbf{E}}ab$
$\mathbb{N}^a ab := \hat{\mathbf{E}}ab$	$\mathbb{Q}^{a/e} ab := \forall z (\Upsilon bz \supset \Pi az)$
$\mathbb{N}^e ab := \mathbf{K}ab$	$\mathbb{Q}^{i/o} ab := \Pi ab$
$\mathbb{N}^i ab := \exists z ((\Upsilon bz \wedge \hat{\mathbf{E}}az) \vee (\Upsilon az \wedge \hat{\mathbf{E}}bz))$	
$\mathbb{N}^o ab := \exists z (\Upsilon bz \wedge \mathbf{K}az) \vee \exists zv (\hat{\mathbf{E}}bz \wedge \hat{\mathbf{E}}av \wedge \forall u (\Upsilon au \wedge \hat{\Sigma}u \supset \mathbf{K}zu))$	